

# Distributed Learning: Sequential Decision Making in Resource-constrained Environments

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# Sequential Decision Making



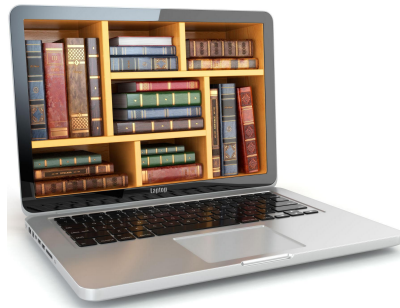
Option 1



Option 2



Option 3



Online Educational  
Systems



Option 4



Option 5



Option 1



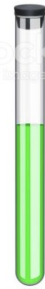
Option 2



Option 3



Option 4

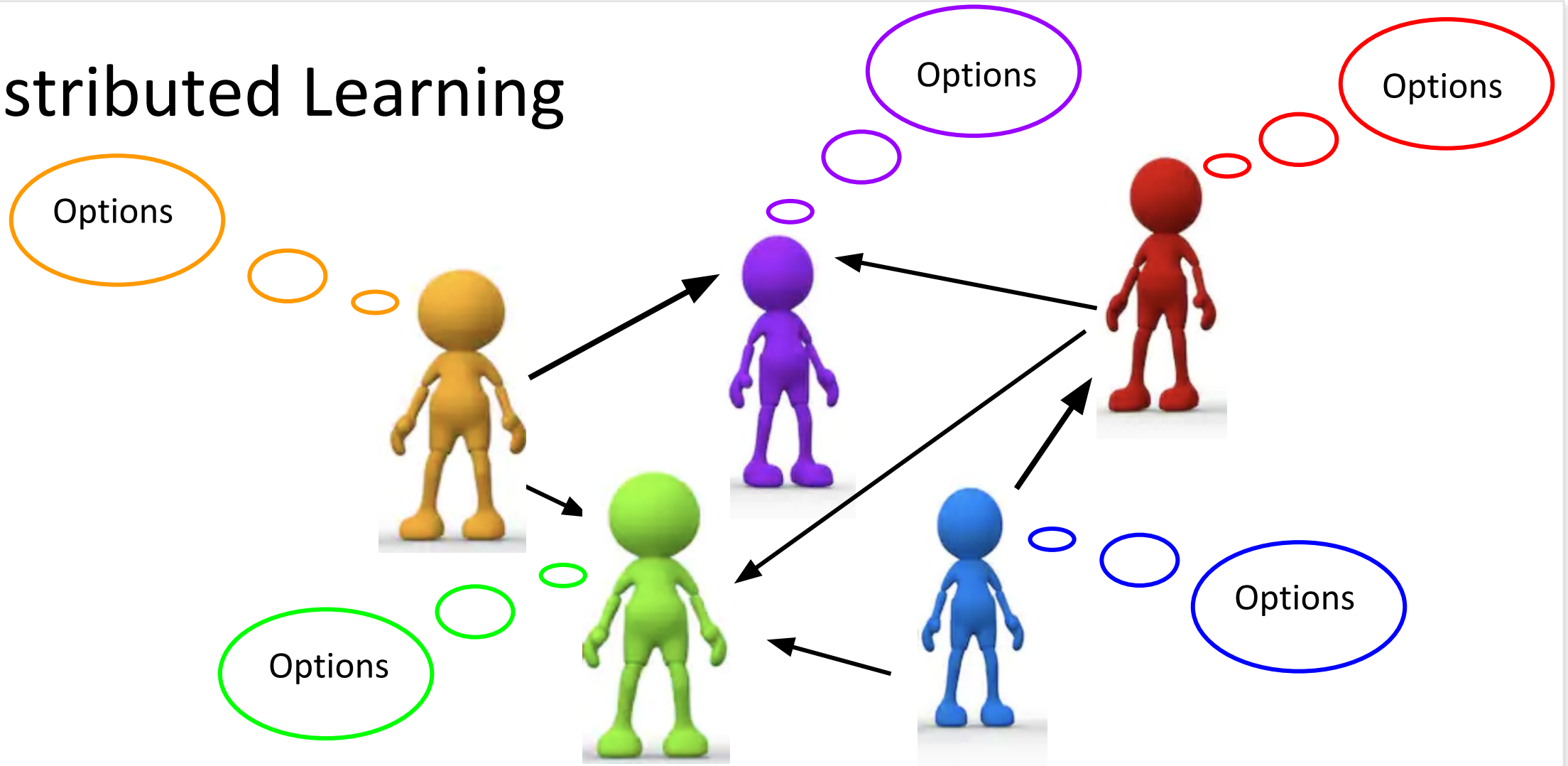



Option 5



Clinical Trials

# Distributed Learning

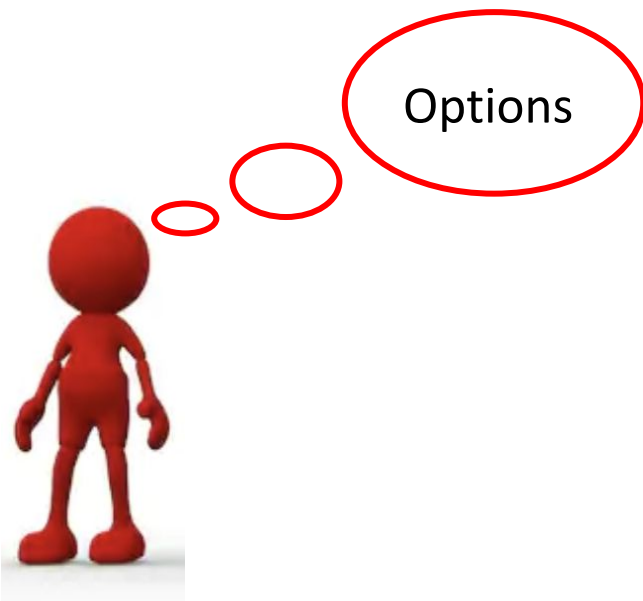




# Distributed Learning Systems

- The goal of each agent is maximizing the individual reward thereby maximizing the group reward.
- Agents communicate with their neighbors, defined according to a network graph.
- We develop a **cost effective partial communication** protocol that obtains **same order of performance as full communication**.

# Sampling Rule



- Estimate the expected reward of options using available information.

$N_i^k(t)$  : Number of Observations

$\hat{\mu}_i^k(t)$  : Average reward

- An option is chosen based on an explore-exploit strategy.

$$Q_i^k(t) = \underbrace{\hat{\mu}_i^k(t)}_{\text{Exploit}} + \underbrace{C_i^k(t)}_{\text{Explore}} : \text{Objective function}$$

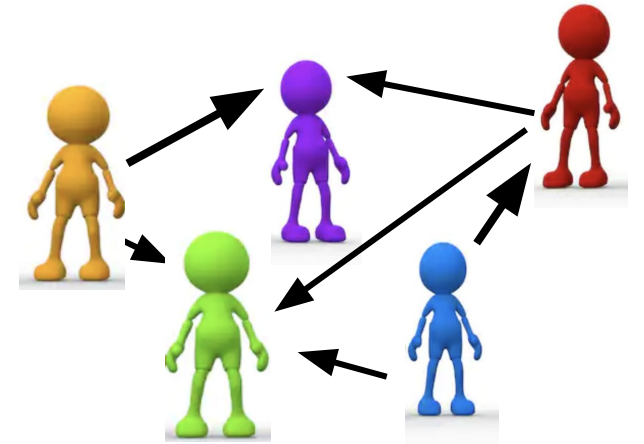
$$\varphi_{t+1}^k = \arg_i \max Q_i^k(t) : \text{Sampling rule}$$

$$\text{with } C_i^k(t) = \sqrt{\frac{\log t}{N_i^k(t)}}$$

# Partial Communication Rules

Agents decide to communicate when they **explore**

$$\varphi_{t+1}^k = \arg_i \max Q_i^k(t) \neq \arg_i \max \hat{\mu}_i^k(t)$$



Rule 1:

Agents **observe** the reward values and actions of their neighbors



Rule 2:

Agents **broadcast** their reward values to their neighbors



Communication cost is **logarithmic** in time

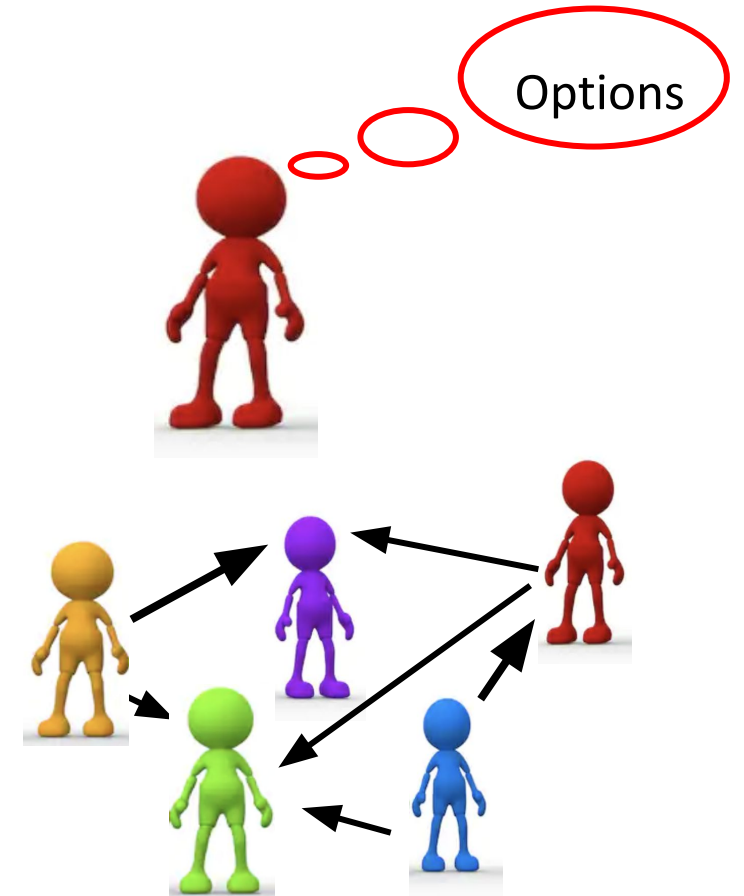
# Performance Analysis

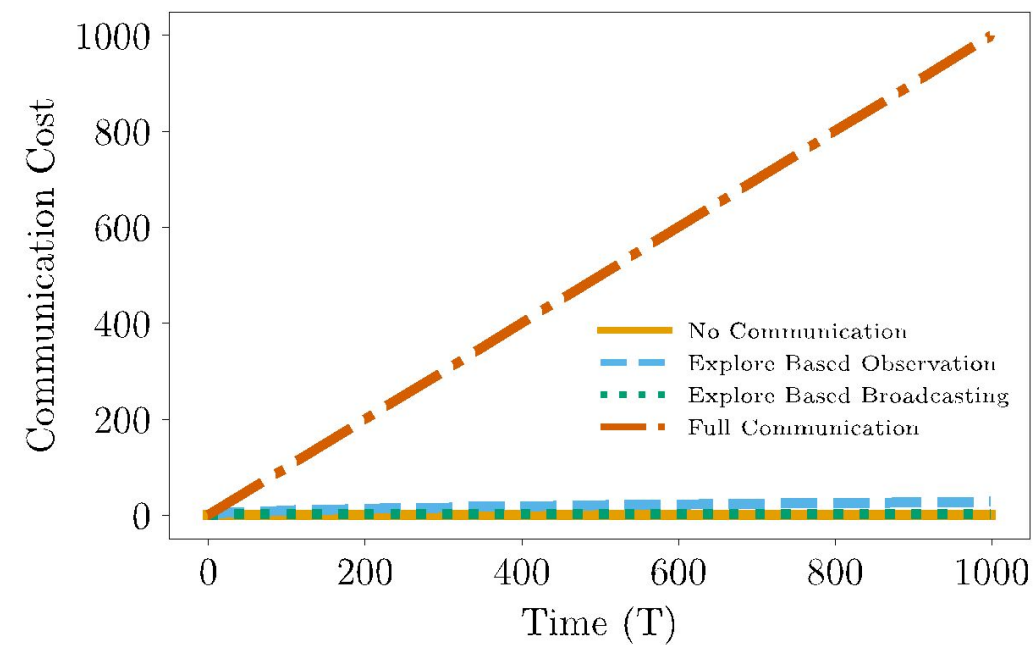
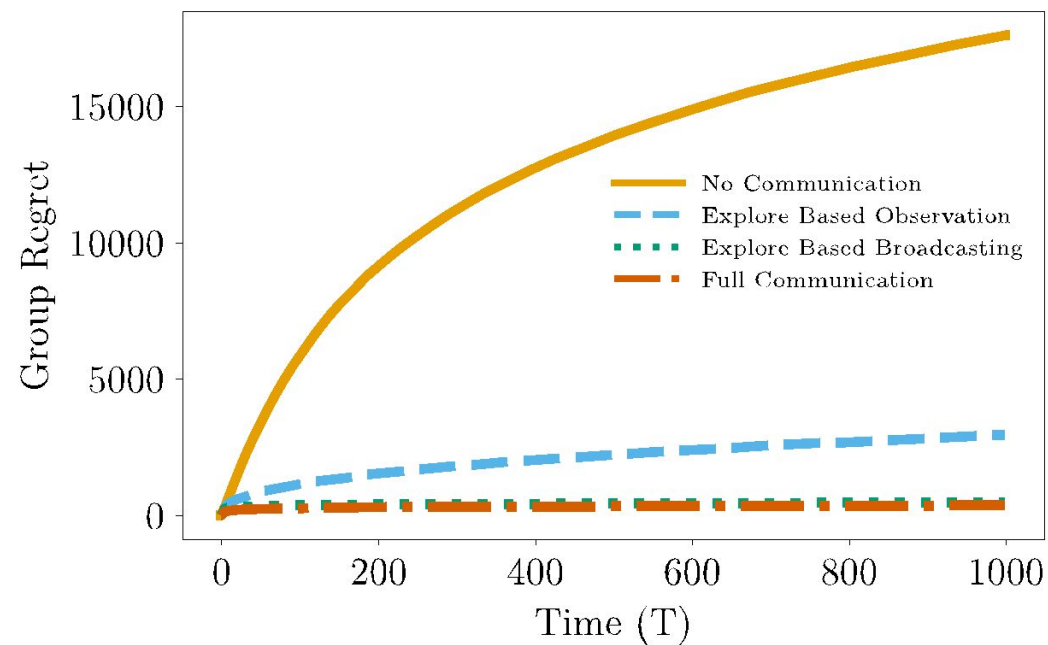
Sampling Regret :

Accumulated expected loss due to sampling suboptimal options.

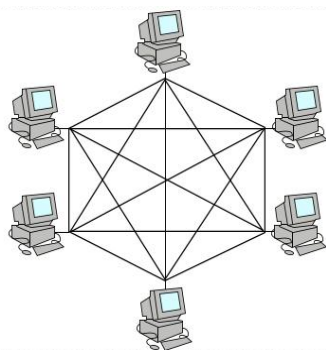
Communication Cost :

Number of times agents communicated.



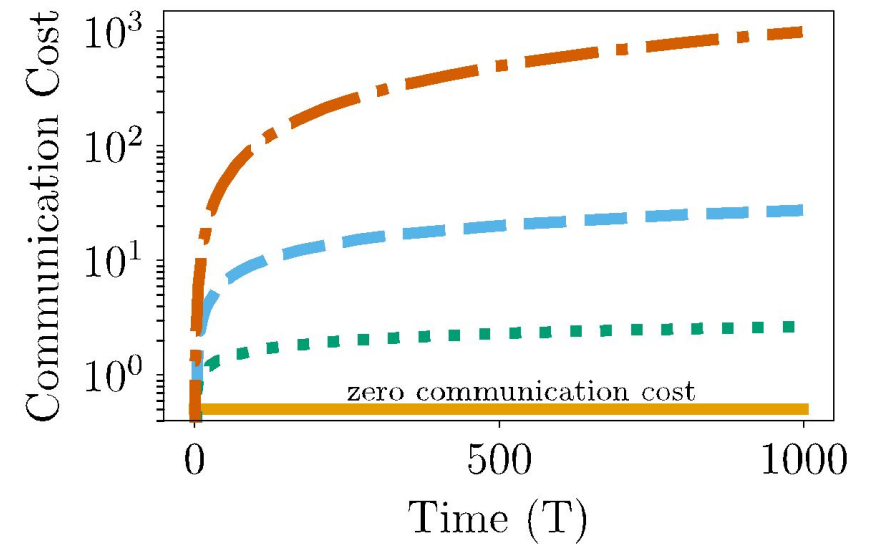
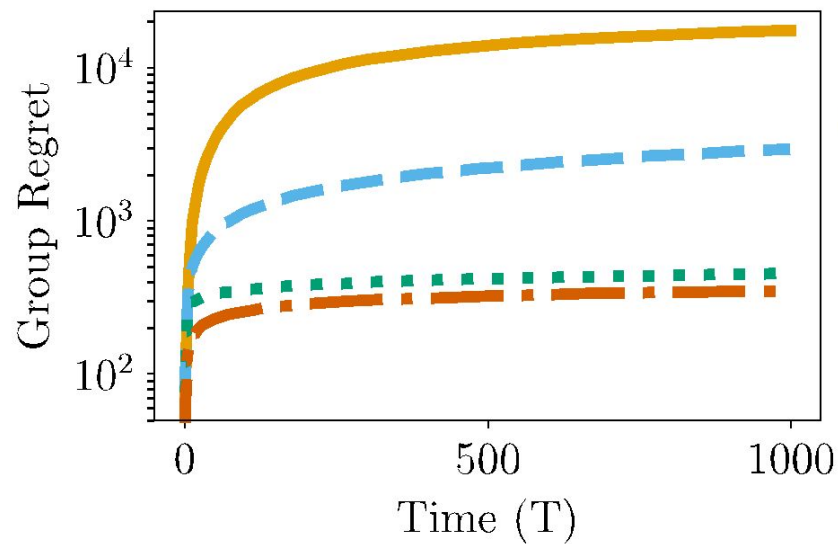


**Complete Graph**

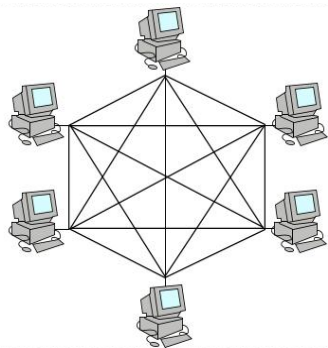


Explore based communication provide significant improvement in performance for a small communication regret





## Complete Graph



Explore based observation provides same order of performance as full communication while utilizing a significantly small communication cost



# Conclusions

- We propose high performance communication protocols that can be utilized in resource-constrained environments.
- Same order of performance as full communication can be obtained by using the proposed partial communication rule
- Communication cost of under the partial communication rule is logarithmic in time. Communication cost under full communication is linear in time.

# Thank You

